ANALYSIS OF WINDING FAULT IN TRANSFORMER WINDING USING TRANSMISSION LINE MODEL

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Abstract: In this paper, an attempt has been made to analyse the frequency response of transformer winding under healthy and faulty conditions (inter-disc short) when very fast transient overvoltages (VFTOs) invades the transformer winding. An algorithm has been developed to incorporate inter-disc faults at different locations of the winding in the transmission line model with frequency dependent loss factor. The resonant frequencies under healthy and faulty conditions are measured using Sweep Frequency Response Analyser. Simulation and measurements are performed on a 22kV prototype continuous disc winding and efficacy of the model is verified by the application of Pearson’s Correlation Coefficient in frequency domain.

1 INTRODUCTION

Gas insulated substation (GIS) has gained a wide range of acceptance in power system for its compactness and high reliability. Switching operations of disconnector switch and circuit breaker within GIS generates very fast transient overvoltages (VFTOs), which are characterized by a very short rise-time of less than 0.1 μs and amplitude of 2.5 p.u. and an oscillatory component of several MHz lasting for tens of micro seconds [1-4]. VFTO could cause oscillations in the voltage inside the transformer connected directly to GIS, since high frequency surges travel more easily along the coaxial gas insulated bus. Due to very short rise time, it can cause an unbalance in voltage distribution in transformer windings. Under these circumstances, the turn-to-turn voltage can rise close to the transformer basic insulation level [8]. Resonance may occur in transformer winding when the frequency of incoming VFTO matches some of the resonant frequencies of the transformer[2]. The VFTOs produced by switching in GIS depends not only on the connection between the GIS and transformer, but also on the transformer parameters and type of the winding [8].

To predict the transient behaviour of the transformer under different types of overvoltages, several models have been reported in the literature. As the efficacy of the model depends on the range of the frequency, it has been reported that the RLC ladder network model can be used for the transients in the frequency range of 10kHz - 1MHz and Transmission Line Model for 1MHz - 5MHz[7]. Single-conductor Transmission Line Model (STLM) and Multi-conductor Transmission Line Model (MTLM) are combined to form a hybrid model to reduce the mathematical complexity with better accuracy. Detailed survey of transformer failure report shows that more than fifty percent of the failures in power transformers are due to the insulation failures in windings [11]. Most of the insulation failures are due to overvoltages of different waveshapes ranging from lightning impulse to VFTO. As the effect of VFTO on transformer winding is more severe under healthy and faulty conditions when compared to lightning impulses, it becomes necessary to use an appropriate model which can simulate winding faults under VFTO. Inter-disc faults at different locations of the winding is analysed in the transmission line model with frequency dependent loss factor. By using Sweep frequency response analyser (FRAX 101, Megger), measurement of the resonant frequencies under healthy and faulty conditions are performed on the 22kV prototype continuous disc winding.

2 TRANSMISSION - LINE MODELS

2.1 Single transmission-line model

In this model, each coil is considered as a transmission line. Figure 1 shows STLM for one-coil system[1]. A sinusoidal voltage of amplitude E₀ and angular frequency ω is applied to the transformer consisting of a single N-turn coil. The average length of each turn in the coil is taken as ‘a’ and the line length is l=a*N. The distributed constants C₀ and C₁ represent the capacitance between the static plates.

Figure 1: Single transmission-line model for one-coil system
The following circuit equation is obtained from figure 1.

\[
\frac{d(V(x))}{dx} = -j\omega[L](I(x)) \tag{1}
\]

\[
\frac{d(I(x))}{dx} = -j\omega[C](V(x)) + j\omega(C_o)E_o \tag{2}
\]

where

\(V(x)\) voltage vector of the coil

\(I(x)\) Current vector of the coil

\([L],[C]\) inductance and capacitance matrices of distributed constants.

The capacitance matrix \(C\) is formed as follows:

\(C_{i,i}\) capacitance of turn 'i' to ground and sum of all other capacitances connected to turn 'i'.

\(C_{i,j}\) capacitance between turns 'i' and 'j' taken with the negative sign.

The inductance matrix \(L\) is calculated through the capacitance matrix \(C\).

\[
[L][C] = \frac{1}{v_s^2} \tag{3}
\]

where, \(v_s\) is the velocity of wave propagation. From the electromagnetic point of view travelling wave propagates through the inter-turn space.

Hence \(v_s\) is calculated as

\[
v_s = \frac{C}{\sqrt{\varepsilon_r}} \tag{4}
\]

where, \(C\) is the speed of light and \(\varepsilon_r\) is the dielectric constant of the transformer insulation. It is pointed out that the matrix in (3) takes into account the mutual inductances within a specific coil.

Substituting equation (3) in equation (1) yields

\[
\frac{d^2(V(x))}{dx^2} = \Gamma^2(V(x)) - kE_0 \tag{5}
\]

Here, \(k = [C_o/(C_o + C_1)]\) indicates the electrostatically induced voltage ratio, \(\Gamma\) is the propagation constant in the wave equation (5). The pure imaginary \(\Gamma\) corresponds to loss free propagation. The solution for eqn. (5) is given by

\[
V(x) = kE_0 + A e^{-\Gamma x} + B e^{\Gamma x} \tag{6}
\]

\[
I(x) = \frac{1}{Z} (A e^{-\Gamma x} - B e^{\Gamma x}) \tag{7}
\]

The first term in equation (6) represents the electrostatically induced voltage. In equation (7), \(Z\) is the characteristic impedance of a turn in a coil defined by

\[
Z_i = \frac{1}{u_s(C_o + C_1 + K) 1 - \cos(\frac{\omega x}{v_s})} \tag{8}
\]

In equation (8), \(K\) is the inter-turn capacitance of the coil, \(\omega\) is the angular frequency of the sinusoidal voltage applied to the transformer coil and \(a\) represents the length of a single turn in the coil. Utilizing the complex dielectric constant and the complex distance reflecting the proximity effect, the following form of \(\Gamma\) is derived:

\[
\Gamma = \frac{1}{v_s} \sqrt{\frac{w}{d}} \left( -\frac{\tan \delta}{2v_s} + j \frac{w}{v_s} \right) \tag{9}
\]

where \(\sigma\) is the conductivity of the conductor, \(\mu\) is the magnetic permeability and \(d\) is the distance between the conductors.

The values of \(A\) and \(B\) in eqns. (6) and (7) are determined from the boundary condition \(V(0) = E_0; V(l) = 0\). Using these values, equations (6) and (7) give the voltage and current distribution in the coil.

The advantage of STLM is that the whole length of the coil is considered as one line and the voltages and currents in the coil are computed by solving a minimal number of equations.

### 2.2 Multi-conductor transmission-line model

MTLM uses the determined voltages in frequency domain from the STLM. Neglecting the magnetic flux in the core, the multi-conductor system without a core is shown in figure 2 employed as in [1].

![Multi-conductor transmission line model for one coil system](image)

Figure 2: Multi-conductor transmission line model for one coil system

The solution of the multi-conductor transmission-line model is similar to that for a single transmission line model given by eqns. (6) and (7).

\[
V_i(x) = kE_0 + A_i e^{-\Gamma x} + B_i \tag{10}
\]
\[ I_i(x) = 1/Z \left( Ae^{-Rx} - Be^{Rx} \right) \]  

(11)

The system of equations (10) and (11) is used to compute the voltages and currents in the turns of a particular coil. The values of \( A_i \) and \( B_i \) are determined by the boundary conditions:

\[ V_i(0) = E_o; \quad V_N(a) = 0; \]
\[ V_i(0) = V_{i+1}(a); \quad I_i(0) = I_{i-1}(a); \]

This is a set of 2N equations for the same number of unknowns \( A_i \) and \( B_i \). The matrix equation from which the vectors \( A_i \) and \( B_i \) can be determined is

\[
\begin{bmatrix}
M_A & M_B \\
M_C & M_D
\end{bmatrix}
\begin{bmatrix}
A \\
B
\end{bmatrix}
= \begin{bmatrix}
(E)_{N+1} \\
(0)_{N+1}
\end{bmatrix}
\]  

(12)

In eqn. (12), \( E \) represents the excitation vector. The description of the matrix elements is given in [2]. The matrix must be solved for each step frequency by providing the voltages at the beginning of the each coil which were previously determined by the STLM. The interturn voltage is defined as the difference between the voltages of two adjacent turns in a coil. The interturn voltage is obtained as \( \delta V = V_i(x) - V_{i+1}(x) \), where \( V_i \) is the voltage in the \( i \)th turn of the studied coil.

The matrices \( M_C, M_D \) in equation (12) can be determined if \( [C] \) matrix is known. \([C]\) Matrix can be computed using the following simple form.

\[
[C] \begin{bmatrix}
C_m + C_i \cdot K \cdot \rho - K \cdot \rho & 0 & \ldots & 0 \\
-K \cdot \rho & (C_i + C_m + 3K) - K \cdot \rho & \ldots & \ldots \\
0 & -K & \ldots & \ldots \\
\ldots & \ldots & \ldots & \ldots \\
0 & \ldots & \ldots & \ldots \\
0 & \ldots & C_i \cdot K & \ldots \\
0 & \ldots & K \cdot \rho & C_i \cdot K \cdot \rho
\end{bmatrix}
\]  

(13)

The values of \( \Gamma \) and \( z_i \) can be evaluated from \( K, C_0, C_1 \) using equations (8) and (9). \( K \) can be easily obtained from the insulation dimension and the rest can be determined from the coil capacitances \( C_m \) and \( C_g \) as shown in figure 3 in the following way.

\[ K_i = \Pi \frac{C_{L(j-1)}^{(i)}}{C_{L(j)}^{(i)} + C_{L}^{(i)}} \]  

(14)

\( C_L^{(i)} \) and \( C_g^{(i)} \) have been shown in figure 3. The total capacitance of coil \( i \) is given by \( C_{H(i)}^{(i)} + C_{L}^{(i)} + C_g^{(i)} \). The equivalent capacitance along the length of the disc \( i \) should be divided by the ratio \( k_i \cdot (1-k) \) to determine \( C_o^{(i)} \) and \( C_i^{(i)} \)

\[
\begin{align*}
C_o^{(i)} &= k_i \cdot \left( C_{L}^{(i)} + C_g^{(i)} \right) / l_i \\
C_i^{(i)} &= (1-k_i) \cdot \left( C_{L}^{(i)} + C_g^{(i)} \right) / l_i
\end{align*}
\]  

(15 a, b)

Figure 3: Equivalent capacitive network of a winding.

3 MTL MODEL OF 22KV PROTOTYPE DISC WINDING

A small change in the parameters can cause significant difference in the results while studying the transient behaviour of the transformer winding under VFTOs. The algorithm of the transmission line model is modified without static plates and a 22kV disc winding is analyzed by using modified algorithm. The physical dimensions and dissipation related constants of the coil are given in table 1.

Figure 2.24: Capacitive voltage distribution

Figure 4 shows the capacitive voltage distribution among the coils of disc winding. Dielectric loss factor in unimpregnated kraft paper is affected by the change of the test frequency. The dielectric constant when measured at lower permissible test temperature, demonstrates its highest variation as the test frequency is increased. At 25°C, the loss factor can be estimated as 0.005 in the frequency band of 0–10 kHz and then it increases with frequency and at 1 MHz it is equal to 0.056[10]. Assuming a drooping variation of transformer insulation loss factor with frequency in the frequency band of 1MHz – 25MHz, a special type of variation, is employed. These variations can
introduce a significant change, especially on the response of the model

Table 1: Parameters of 22 kV disc winding

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Turn Length (a)</td>
<td>1m</td>
</tr>
<tr>
<td>Number of turns (N)</td>
<td>12</td>
</tr>
<tr>
<td>Number of discs (Nc)</td>
<td>40</td>
</tr>
<tr>
<td>Dielectric constant of insulation (εr)</td>
<td>2.08</td>
</tr>
<tr>
<td>Distance between the conductor (d)</td>
<td>0.3125mm</td>
</tr>
<tr>
<td>Section clearance</td>
<td>3mm</td>
</tr>
<tr>
<td>Height of section (axial)</td>
<td>313mm</td>
</tr>
<tr>
<td>Depth of winding (radial)</td>
<td>19.5mm</td>
</tr>
<tr>
<td>Conductor conductivity (σ)</td>
<td>5 x 10⁷ S/m</td>
</tr>
<tr>
<td>Permeability (μ=μo)</td>
<td>4πx10⁻⁷ H/m</td>
</tr>
<tr>
<td>Surge velocity (us)</td>
<td>208 m /μs</td>
</tr>
<tr>
<td>Dielectric loss factor (tan δ)</td>
<td>0.02</td>
</tr>
<tr>
<td>Coil capacitance (Cm)</td>
<td>2.23pF</td>
</tr>
<tr>
<td>Ground Capacitance (Cg)</td>
<td>11.65pF</td>
</tr>
<tr>
<td>Interturn Capacitance (K)</td>
<td>147.8pF</td>
</tr>
</tbody>
</table>

4 FREQUENCY DOMAIN ANALYSIS OF HEALTHY WINDING

The voltage distribution of 22 kV disc winding is computed by MTL model. Continuous disc winding has 40 discs and each disc has 12 turns in it. The schematic diagram of the disc winding is shown in the figure 5. Tappings were brought out at every 4 disc (4 disc is 10% of the winding) and 2 disc (2.5% of the winding) in order to create inter disc short fault.

![Figure 5: Schematic diagram of the disc winding](image)

Figure 5: Schematic diagram of the disc winding

Figure 6: Frequency characteristics of voltage across coil 5

Figure 7: Frequency characteristic of voltage across coil 9

Frequency characteristic of voltage across coil 5 and coil 9 are shown in figure 6 and 7 respectively. (a) and (b) represents the measured value and the simulated value respectively.

4.1 Verification Using Pearson’s Correlation Coefficient

Correlation is a useful technique to investigate the relationship between two quantitative, continuous variables. It measures the strength and direction of a linear relationship between two variables. This correlation coefficient is presented by the following equation:

\[
    r = \frac{\sum_{i=1}^{n} \left( U_{mi} - \bar{U}_m \right) \left( U_{si} - \bar{U}_s \right)}{\sqrt{\sum_{i=1}^{n} \left( U_{mi} - \bar{U}_m \right)^2 \left( U_{si} - \bar{U}_s \right)^2}}
\]

where \( U_m \) is the measured value of variable and \( U_s \) is its simulated value. \( r \) could be a number between -1 and 1. A positive value of \( r \) means a positive linear relationship; a negative value of means a negative linear relationship. The correlation is ideal as \( r \) approaches 1 and it is not desirable to approach -1. [7]

Table 2: Pearson’s correlation coefficient for MTL model for healthy winding

<table>
<thead>
<tr>
<th>Disc No.</th>
<th>tanδ const (0.02)</th>
<th>tanδ varying</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>0.254</td>
<td>0.254</td>
</tr>
<tr>
<td>2</td>
<td>0.761</td>
<td>0.764</td>
</tr>
<tr>
<td>5</td>
<td>0.622</td>
<td>0.625</td>
</tr>
<tr>
<td>9</td>
<td>0.489</td>
<td>0.494</td>
</tr>
<tr>
<td>13</td>
<td>0.393</td>
<td>0.4</td>
</tr>
<tr>
<td>17</td>
<td>0.311</td>
<td>0.32</td>
</tr>
<tr>
<td>21</td>
<td>0.23</td>
<td>0.24</td>
</tr>
<tr>
<td>25</td>
<td>0.156</td>
<td>0.168</td>
</tr>
<tr>
<td>29</td>
<td>0.07</td>
<td>0.084</td>
</tr>
<tr>
<td>Average</td>
<td>0.365</td>
<td>0.372</td>
</tr>
</tbody>
</table>
Considering the results shown in table 2 the accuracy of the MTL model can be studied. Due to the nonlinearity in voltage distribution as shown in figure 3 the coefficient has been shown upto only 70% of the winding. A relatively good correlation observed between the computed and measured voltages with frequency-dependent loss factor.

5 FREQUENCY DOMAIN ANALYSIS OF INTERDISC FAULT WINDING

Interdisc shorts are created at different positions of the disc winding. The voltage distribution of 22 kV disc winding with fault is computed by MTL model. Voltages at different disc terminals are simulated and measured by means of Sweep frequency response analyser (FRAX 101, Megger). Fault of 2.5% of the winding is done by shorting the first and second disc. Fault of 10% and 20% of the winding are done by shorting first to fifth disc and first to ninth respectively. The voltage distribution in coil 5 with 2.5% of winding shorts is shown figure 8. The voltage distributions in coil 13 with 10% and 20% of winding shorts are shown in figure 9 and 10 respectively.

<table>
<thead>
<tr>
<th>Fault Percentage</th>
<th>Discs</th>
<th>Correlation Coefficient</th>
</tr>
</thead>
<tbody>
<tr>
<td>2.5%</td>
<td>6</td>
<td>0.792</td>
</tr>
<tr>
<td>10%</td>
<td>9</td>
<td>0.522</td>
</tr>
<tr>
<td>20%</td>
<td>13</td>
<td>0.394</td>
</tr>
<tr>
<td></td>
<td>17</td>
<td>0.299</td>
</tr>
<tr>
<td></td>
<td>21</td>
<td>0.202</td>
</tr>
<tr>
<td></td>
<td>25</td>
<td>0.123</td>
</tr>
<tr>
<td></td>
<td>29</td>
<td>0.031</td>
</tr>
<tr>
<td>Average</td>
<td>0.338</td>
<td>0.283</td>
</tr>
</tbody>
</table>

Table 3: Pearson’s correlation coefficient for MTL model for inter disc fault winding

With fault, resonant frequencies of the transformer are getting shifted. Table 4 and 5 shows the shift in resonant frequencies of coil 13 with 2.5% and 10% of fault respectively.

<table>
<thead>
<tr>
<th>Measured resonant frequency using SFRA (MHz)</th>
<th>Simulated resonant frequency using MATLAB (MHz)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Healthy</td>
<td>2.5% Fault</td>
</tr>
<tr>
<td>6.347</td>
<td>0.359</td>
</tr>
<tr>
<td>1.67</td>
<td>1.93</td>
</tr>
<tr>
<td>2.67</td>
<td>3.06</td>
</tr>
<tr>
<td>3.94</td>
<td>4.03</td>
</tr>
<tr>
<td>4.53</td>
<td>4.63</td>
</tr>
<tr>
<td>5.5</td>
<td>5.57</td>
</tr>
<tr>
<td>6.69</td>
<td>6.77</td>
</tr>
<tr>
<td>8.05</td>
<td>8.53</td>
</tr>
<tr>
<td>9.68</td>
<td>9.79</td>
</tr>
</tbody>
</table>

Table 4: Shift in Resonant Frequencies of coil 13 with 2.5% Fault

<table>
<thead>
<tr>
<th>Measured resonant frequency using SFRA (MHz)</th>
<th>Simulated resonant frequency using MATLAB (MHz)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Healthy</td>
<td>10% Fault</td>
</tr>
<tr>
<td>0.184</td>
<td>0.19</td>
</tr>
<tr>
<td>0.347</td>
<td>0.364</td>
</tr>
<tr>
<td>0.417</td>
<td>0.437</td>
</tr>
<tr>
<td>1.68</td>
<td>2.46</td>
</tr>
<tr>
<td>2.66</td>
<td>2.9</td>
</tr>
<tr>
<td>4.63</td>
<td>5.02</td>
</tr>
<tr>
<td>7.6</td>
<td>7.9</td>
</tr>
<tr>
<td>10.9</td>
<td>11.2</td>
</tr>
</tbody>
</table>

Table 5: Shift in Resonant Frequencies of coil 13 with 10% Fault
There is good agreement between measured and simulated value. Table 3 shows Pearson’s correlation coefficients for different percentage of faults in which the coefficients are taken between the measured and simulated value at different discs.

6 CONCLUSION

This paper presents the interdisc fault analysis of a 22kV prototype continuous disc winding using MTL model for very fast transient studies and the simulation results have been compared with the measurement results. The efficacy of the model is verified by the application of Pearson’s Correlation Coefficient in frequency domain. A relatively good correlation observed between measurement and MTL model with a frequency-dependent loss factor variation, provides a better agreement between the computed and the measured voltages. It has been shown that there will be minimum shift of 1.2% in resonant frequencies with 2.5% fault and 2.68% with 10% fault compared to healthy condition.

7 REFERENCES


